

# TENTH LECTURE SUMMARY

## TEST OF INDEPENDENCE

OF TWO VARIABLES (ATTRIBUTES) BOTH TYPICALLY (BUT NOT NECESSARILY) OF THE **NOMINAL-SCALE** TYPE.

**SAMPLE** IS USUALLY SUMMARIZED IN A **CONTINGENCY TABLE**, E.G.

GRADE6 9YEAR	A	B	C	D	
I	23 21.66	15 16.74	17 15.95	9 9.65	64
II	56 57.20	48 44.20	39 44.20	26 25.48	169
III	31 31.14	22 24.06	25 22.93	14 13.87	92
	110	85	81	49	325

WHERE WE CAN DISPLAY BOTH THE **OBSERVED** AND **EXPECTED** (**CALCULATED**) FREQUENCIES OF EACH **CELL**.

**NULL HYPOTHESIS** STATES THAT THE TWO VARIABLES ARE **INDEPENDENT** (THE DISTRIBUTION OF GRADES DOES NOT CHANGE WITH YEAR OF STUDY).

**TEST STATISTIC** COMPUTED BY  $\sum \frac{(O-E)^2}{E}$

I.E.  $\frac{(23-21.66)^2}{21.66} + \frac{(15-16.75)^2}{16.75} + \dots + \frac{(14-13.87)^2}{13.87} = 1.335$

AND COMPARED AGAINST THE CRITICAL VALUE OF THE **CHI-SQUARE** DISTRIBUTION WITH  $(\#R - 1) \times (\#C - 1)$  DEGREES OF FREEDOM (ALWAYS A **RIGHT TAIL** TEST).

## **GOODNESS-OF-FIT TEST**

CONCERNS A SINGLE NOMINAL-SCALE VARIABLE WITH A HANDFUL OF POTENTIAL VALUES. THE INDIVIDUAL **PROBABILITIES** OF THESE ARE SPECIFIED BY THE **NULL HYPOTHESIS**, E.G.

GRADE	A	B	C	D
OBSERVED	110	85	81	49
$H_0$ : Prob =	35%	25%	25%	15%
<b>EXPECTED</b>	<b>113.75</b>	<b>81.25</b>	<b>81.25</b>	<b>47.25</b>

**EXPECTED FREQUENCIES** ARE COMPUTED BY MULTIPLYING EACH **PROBABILITY** OF  $H_0$  BY  $n$  (TOTAL OF OBSERVED FREQUENCIES).

**TEST STATISTIC** IS COMPUTED USING THE

SAME  $\sum \frac{(O-E)^2}{E}$ , I.E.

$$\frac{(110-113.75)^2}{113.75} + \dots + \frac{(49-47.25)^2}{47.25} = 0.363$$

AND COMPARED TO **CRITICAL VALUE** OF **CHI-SQUARE** DISTRIBUTION WITH  $k - 1$  DEGREES OF FREEDOM (**CRITICAL REGION** CONSISTS AGAIN OF THE **RIGHT TAIL** ONLY), WHERE  $k$  IS THE NUMBER OF '**CELLS**', I.E. POTENTIAL VALUES.