

TWELFTH LECTURE SUMMARY

NONPARAMETRIC TESTS

DON'T REQUIRE THE POPULATION(S) TO BE NORMAL, NOR SAMPLE SIZE(S) TO BE LARGE ($n > 30$)

ARE, IN GENERAL, **LESS POWERFUL** THAN THEIR PARAMETRIC COUNTERPARTS (I.E. THEY ARE LESS LIKELY TO REJECT H_0 WHEN THE POPULATION DIFFERENCES ARE NOT VERY PRONOUNCED)

WE DISCUSSED **THREE SPECIFIC CASES:**

SIGN TEST

USED IN THE **PAIRED-SAMPLES** (BEFORE AND AFTER) SITUATION, WHEN DIFFERENCES CANNOT BE CONSIDERED NORMAL (AND $n \neq 30$)

WE KEEP ONLY THE **SIGN** OF THE DIFFERENCES, DISCARDING **N.D.** (ZERO DIFFERENCE) OBSERVATIONS (CORRESPONDINGLY **REDUCING** THE VALUE OF n)

H_0 STATES THAT THE POPULATION PROPORTION OF THE **+** SIGNS EQUALS $\frac{1}{2}$,
 H_1 CAN BE ANY OF THE USUAL 3 CHOICES

TEST STATISTIC:
$$\frac{x - 0.5}{\sqrt{\frac{0.25}{n}}}$$

WHERE x IS THE PROPORTION OF **+** SIGNS (THE OLD \hat{p}) AND n IS THE **REDUCED** SAMPLE SIZE

WE ALREADY KNOW THAT, WHEN $n > 10$ **AND THE NULL HYPOTHESIS IS TRUE**, THIS TEST STATISTIC HAS THE **STANDARD NORMAL** DISTRIBUTION (z); WE FIND THE CRITICAL VALUES ACCORDINGLY

RANK-SUM (MANN-WHITNEY) TEST

USED IN THE CASE OF TWO INDEPENDENT SAMPLES, TESTING $H_0: \mu_1 = \mu_2$ AGAINST ONE OF THE USUAL ALTERNATES

ASSUMPTION: SAME-SHAPE POPULATIONS (DIFFERENT FROM TEXTBOOK)

WE REQUIRE EACH SAMPLE TO HAVE AT LEAST EIGHT OBSERVATIONS

COMPUTATION OF TEST STATISTIC:

RANK THE VALUES OF POOLED SAMPLES (FROM 1 TO n_1+n_2), KNOW HOW TO DEAL WITH TIES

SUM THE RANKS OF THE SAMPLE-ONE OBSERVATIONS (CALL THIS SUM R)

CONVERT TO
$$\frac{R - \mu_R}{\sigma_R}$$

WHERE $\mu_R = n_1 \frac{n_1 + n_2 + 1}{2}$

(THE EXPECTED VALUE OF R WHEN H_0

HOLDS), AND $\sigma_R = \sqrt{\frac{n_1 n_2 (n_1 + n_2 + 1)}{12}}$

(THE CORRESPONDING STANDARD DEVIATION).

SPEARMAN (RANK) CORRELATION COEFFICIENT

USED IN SITUATIONS OF CHAPTER 10
(DOES THE RESPONSE VARIABLE y
INCREASE OR DECREASE WITH x) WHEN
THE RELATIONSHIP IS NOT NECESSARILY
LINEAR

TO COMPUTE r_s WE FIRST NEED TO RANK,
INDIVIDUALLY, x AND y OBSERVATIONS

(TO SIMPLIFY THE ISSUE, YOUR TEXTBOOK SKIPS THIS STEP, ASSUMING THAT BOTH SETS OF OBSERVATIONS ARE ALREADY PRESENTED IN THEIR RANKED FORM)

THEN SUBTRACT THE y RANKS FROM THE x RANKS (d STANDS FOR THE RESULTING DIFFERENCES) AND COMPUTE

$$r_s \equiv 1 - \frac{6 \sum d^2}{n(n^2 - 1)}$$

WHERE n IS THE NUMBER OF THESE DIFFERENCES (THIS TIME, ZERO DIFFERENCES COUNT)

USING THIS r_s , WE CAN TEST (TABLE 9)

H_0 : THERE IS NO CORRELATION BETWEEN x AND y

H_1 : THERE IS A POSITIVE CORRELATION (OR THE OTHER TWO ALTERNATIVES)