MATH2F05 FIRST MIDTERM NOVEMBER 7, 2005 Full credit given for three correct and complete answers. Open-book exam. Duration: 50 minutes

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Find general solution to:

1. 
$$(y^3 + 2xe^y)y' = ye^y$$
 Hint:  $x \leftrightarrow y$ 

2. 
$$x^2y'' - 3xy' + 4y = x \ln x$$

3. 
$$x^2y' + (2x - 1)y + x^2y^2 = 0$$

$$4. \ y'' = \frac{y'}{x} \left( 1 + \ln \frac{y'}{x} \right)$$

5. 
$$\left(y\cos\frac{x}{y} + 2xy^2\right)dx = \left(x\cos\frac{x}{y} + y^2\right)dy$$

Hint: Find integrating factor