

1. ..

(a)

$$\Pr[(A \cap \bar{B}) \cup (B \cap C) \cup (C \cap \bar{D})] = \Pr(A) \Pr(\bar{B}) + \Pr(B) \Pr(C) + \Pr(C) \Pr(\bar{D}) - \\ - \Pr(A) \Pr(\bar{B}) \Pr(C) \Pr(\bar{D}) - \Pr(B) \Pr(C) \Pr(\bar{D}) = \dots$$

(b)

$$\Pr[(\bar{A} \cup B) \cap \overline{B \cup C} \cap (\bar{C} \cup D)] = 1 - \Pr[(A \cap \bar{B}) \cup B \cup C \cup (C \cap \bar{D})] \\ = 1 - \Pr[(A \cap \bar{B}) \cup B \cup C] = 1 - \Pr(A) \Pr(\bar{B}) - \Pr(B) - \Pr(C) + \\ + \Pr(A) \Pr(\bar{B}) \Pr(C) + \Pr(B) \Pr(C) = \dots$$

2.

(a)

$$\sum_{i=-1}^2 \sum_{j=\max(1,i)}^{|i|+2} (2i^2 + j + 1) = 71 \\ \frac{1}{71} \sum_{i=-1}^2 \sum_{j=\max(1,i)}^{|i|+2} i(2i^2 + j + 1) = \frac{72}{71} \\ \frac{1}{71} \sum_{i=-1}^2 \sum_{j=\max(1,i)}^{|i|+2} j(2i^2 + j + 1) = \frac{182}{71} \\ \frac{1}{71} \sum_{i=-1}^2 \sum_{j=\max(1,i)}^{|i|+2} (i - \frac{72}{71})(j - \frac{182}{71})(2i^2 + j + 1) = 0.4991$$

(b)

X	$Y = 2$	-1	1	2
\Pr		$\frac{6}{24}$	$\frac{6}{24}$	$\frac{12}{24}$

$$-3 \cdot \frac{6}{24} - 3 \cdot \frac{6}{24} + 0 \cdot \frac{12}{24} = -1.5$$

3.

(a) Introducing A , B and C for this happening in rolls $(1, 2)$, $(2, 3)$ and $(3, 4)$, we get

$$\Pr(A \cup B \cup C) = \frac{1}{36} + \frac{1}{36} + \frac{1}{36} - \frac{1}{6^4} = 8.256\%$$

(b) Breaking it down according to where the first 6 occurred:

$$\frac{1}{6}(1 - \frac{5^3}{6^3}) + \frac{5}{6} \cdot \frac{1}{6}(1 - \frac{5^2}{6^2}) + (\frac{5}{6})^2 \frac{1}{6} \cdot \frac{1}{6} = 13.19\%$$

4.

(a)

$$\begin{aligned} \mu &= 1.35 \\ \sigma &= 2.475 \\ \text{skewness} &= 0.9212 \end{aligned}$$

(b)

20.10

5.

0S, >3	$\frac{\binom{39}{3}}{\binom{52}{3}} \cdot 0 = 0$
1S, >3	$\frac{\binom{39}{2} \cdot 13}{\binom{52}{3}} \cdot \frac{3}{6} = \frac{741}{3400}$
2S, >3	$\frac{39 \cdot \binom{13}{2}}{\binom{52}{3}} \cdot (1 - \frac{3}{36}) = \frac{429}{3400}$
3S, >3	$\frac{\binom{13}{3}}{\binom{52}{3}} \cdot (1 - \frac{1}{6^3}) = \frac{473}{36720}$

(a)

$$\frac{741}{3400} + \frac{429}{3400} + \frac{473}{36720} = 35.70\%$$

(b)

$$\frac{\frac{429}{3400} + \frac{473}{36720}}{\frac{741}{3400} + \frac{429}{3400} + \frac{473}{36720}} = 38.95\%$$

6. ..

(a)

$$\begin{aligned} \mu &= -0.5385 \text{ dollars} \\ \sigma &= 2.713 \text{ dollars} \end{aligned}$$

(b)

65.31%

7.

(a)

-5
8.660

(b)

59.16%