

1. Using Runge-Kutta technique and  $h = 0.01$ , find a solution to the following set of differential equations

$$\begin{aligned}\dot{x} &= 10(y - x) \\ \dot{y} &= 28x - y - xz \\ \dot{z} &= xy - \frac{8}{3}z\end{aligned}$$

for  $t$  (the independent variable) from 0 to 20, where  $x(0) = 1$ ,  $y(0) = 2$  and  $z(0) = 3$ . Display the corresponding path in a 3-dimensional picture.

2. Similarly, solve

$$\ddot{y} + y - \dot{y}(1 - y^2) = 0$$

for  $t$  from 0 to 10, where  $y(0) = 1$  and  $\dot{y}(0) = 2$ . Display  $y$  as a function of  $t$ . How close can you get to the two initial values by reversing the direction of time and 'backtracking' to  $t = 0$ .

Optional: Repeat the same, with  $t$  going from 0 to 20.