

1. Five cards are randomly dealt from a regular deck of 52 cards. Then, a die is rolled until getting as many sixes as the number of spades dealt (when this number is zero, the die is not rolled at all). Compute
 - (a) the expected number of rolls and the corresponding standard deviation,
 - (b) the probability that the die will have to be rolled more than 20 times.
2. Consider a branching process which starts with 9 initial members and has the following offspring distribution

number	0	1	2	3	4	5	6
Pr	0.503	0.213	0.149	0.083	0.032	0.017	0.003

Find

- (a) the expected number of members of Generation 18 and the corresponding standard deviation,
- (b) the probability that Generation 18 will have more than 11 members,
- (c) the probability that extinction will take more than 18 generations,
- (d) the expected number of generations till extinction, and the corresponding standard deviation.
- (e) the expected number of members of the process who will have ever lived up to and including Generation 18, and the corresponding standard deviation,
- (f) the probability that this number will be bigger than 150,
- (g) the expected number of *total* progeny of this process (till its eventual extinction), and the corresponding standard deviation,
- (h) the probability that this number will be bigger than 150.